

TQFTs in the BV-BFV Formalism and Deformation Quantization

Habilitationsschrift

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2	Formal Global Perturbative Quantization of the Rozansky–Witten Model in the BV-BFV Formalism Journal of Geometry and Physics, Volume 174, (2022)	122
3	Convolution Algebras for Relational Symplectic Groupoids and Reduc- tion Pacific Journal of Mathematics, Volume 313.1, pp. 75–102, (2021)	151
4	On Quantum Obstruction Spaces and Higher Codimension Gauge The- ories Physics Letters B, Volume 815, (2021)	183
5	Formal Global AKSZ Gauge Observables and Generalized Wilson Sur- faces Annales Henri Poincaré, Volume 21, pp. 2951–2995, (2020)	204
6	Computation of Kontsevich Weights of Connection and Curvature Graphs for Symplectic Poisson Structures Advances in Theoretical and Mathematical Physics, Volume 25.5, (2021)250	