

Chiral Vibrational Spectroscopy with the Nuclear Velocity Perturbation Theory and the Magnetic Field Perturbation Theory

Dissertation

zur

Erlangung der naturwissenschaftlichen Doktorwürde

(Dr. sc. nat.)

vorgelegt der

Mathematisch-naturwissenschaftlichen Fakultät

der

Universität Zürich

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Zürich, 2023

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