

**DMK | Deutschschweizerische Mathematikkommission des VSMP**  
(Verein Schweizerischer Mathematik- und Physiklehrkräfte)

# **Stochastics**

**Theory and Exercises  
for ‘Sekundarstufe II’**

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